

# Numerical Simulation of Flame Acceleration and Fast Deflagrations Using Artificial Thickening Flame Approach

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## 1 Introduction

The numerical studies of flame acceleration and fast deflagrations in an obstructed channel were carried out widely over the past ten years [1-4]. Most of these high resolution numerical simulations used a single-step Arrhenius reaction model and no explicit turbulent model were used. So it seems that the turbulence field in the unburned gas ahead of the flame was under-resolved [5]. Johansen and Ciccarelli [5] carried out large eddy simulations of initial flame acceleration using a flame surface density (FSD) combustion model. They showed the turbulent flame finally enters the “thickened reaction zones” regime during the initial stages of the flame acceleration. In this regime the rate of combustion is more controlled by the rate of chemical reactions than the rate of mixing. Hence, to model the propagation of fast deflagrations in an obstructed channel the artificially thickened flame (ATF) approach [6] which is based on the Arrhenius model seems to be an appropriate option. In this model, it is implicitly assumed that the chemistry rather than mixing control the reaction rate [6]. In this approach, sub-grid turbulent mixing is also included using the efficiency function [7]. Another issue was commented by Kessler et al. [3] is that the single step Arrhenius model cannot be used for calculating properties of flames for which diffusion and thermal conduction are important. This model may not be appropriate for combustion wave transitions, such as the transition from a laminar to turbulent flame or a turbulent flame to a detonation. Hence, a more complete chemical reaction model is needed. Therefore in this paper the two-dimensional filtered reactive Navier-Stokes equations were solved utilising chemistry base combustion model (i.e. ATF approach) and using detailed chemical kinetic.

## 2 Simulation Setup

The basic idea of the ATF approach is to artificially thicken the premixed flame so that the flame front can be resolved on a coarse grid while keeping the laminar flame speed

$S_i^0$  constant. This is achieved by increasing the molecular diffusion coefficient ( $D$ ) by a thickening factor ( $F$ ), whereas the pre-exponential factor of the Arrhenius law ( $A$ ) is decreased by this factor [8]. Hence, the flame thickness is multiplied by  $F$  ( $\delta_1^1 = F\delta_1^0$ ) while the laminar flame speed remains unchanged [8]. The value of the thickening factor  $F$  is typically chosen such that the thickened flame structure can be resolved on 10 computational cells (i.e.  $\delta_1^1 \cong 10\Delta_x$ ) [7]. Since the thickened flame is much thicker than the length scales of most part of the turbulent eddies in the flow, these eddies do not lead to noticeable flame wrinkling. To overcome this drawback, the thickened flame speed is corrected using an efficiency function,  $E$ . In fact, the efficiency function can be considered as a sub-grid model to account for the interaction of the flame and turbulence [7]. In the present work, the efficiency function proposed by Colin et al. [7] is used. In LES/ATF model, the species conservation equation is written as:

$$\frac{\partial(\rho Y_k)}{\partial t} + \frac{\partial(\rho \tilde{u}_j Y_k)}{\partial x_j} = \frac{\partial}{\partial x_j} \left( \rho DEF \frac{\partial Y_k}{\partial x_j} \right) + \frac{\dot{\omega}_k}{F},$$

where  $u_j$ ,  $\rho$ ,  $Y_k$  and  $\dot{\omega}_k$  are the components of the velocity field, density, mass fraction and reaction rate of species  $k$ , respectively. The superscript ( $\sim$ ) denotes a mass-weighted filtered quantity. The same modifications were also implemented for the energy equation.

The LES/ATF model has been applied widely to premixed and partially premixed flames in different configurations with reasonable accuracies (e.g. [9, 10]). Xiao et al. [9] studied a premixed hydrogen/air flame propagation and tulip flame formation in a closed channel using the ATF model and a detailed chemistry. They reported that the flame velocity and pressure during the transient combustion have been well reproduced. Quillatre et al. [10] have shown that using a two-step chemical mechanism, the LES/ATF model accurately reproduce the subsonic flame propagation past repeated obstacles and over-pressure generated in an explosion chamber. In a very recent work of Yu and Navarro-Martinez [11] the effect of thickening procedure on the DDT of shock-flame interaction was studied. They reported that the ATF approach captures the relevant physics and detonation times and lengths are quasi mesh independent [11].

In the present LES simulation, the SGS turbulent viscosity is modeled as a function of the filter size and the SGS turbulent kinetic energy that described by a transport equation. In addition the detailed kinetic mechanism was used for stoichiometric hydrogen-air mixture. This mechanism involved 9 species and 27 steps. Also In-situ adaptive tabulation (ISAT) method was also exploited to reduce the computational cost due to the detailed chemistry. A second order bounded central scheme is used for diffusion and pressure gradient terms in the governing equations. To avoid numerical dissipation and dispersion a total variation diminishing (TVD) scheme, using the Sweby flux limiter is used for discretization of the convective terms. To treat the pressure-velocity coupling a standard iterative procedure (i.e. PISO algorithm) is employed.

The computational domain is a 2D channel with a length of 64 cm and a width of 4 cm [1, 2] (Fig. 1). The channel is obstructed by rectangular obstacles with a width of  $d/16$  and height of  $d/4$ , where  $d$  is the channel width. First obstacle is placed at a distance of  $d/2$  from the closed end and the others are equally spaced at a distance  $d$ . The obstacles have blocked the half of the channel width, so that the blockage ratio is 0.5.

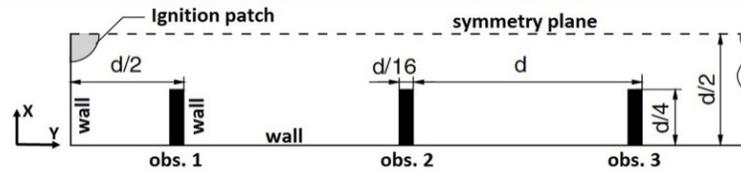


Figure 1. Schematic of combustion chamber.

### 3 Verification of the Results

In this section the accuracy of the results in production of the flame speed is verified against the previous studies. In this study a uniformly structured computational grid was used with the cell size of 0.0625 mm. This translates to have 5-6 cells per laminar flame thickness. Furthermore, using a proper artificial thickening factor, the flame front will be resolved here. To verify the present work, a comparison between the present results with those of Gamezo et al. [1] has been shown in Fig. 2. In this figure, the flame tip speed is plotted versus time. A good agreement is observed between the present results with those of Gamezo et al. [1]. It should be pointed out that since the flame acceleration occurs sooner in the numerical experiment of Gamezo et al. [1], for better comparison, the present results are shifted 0.65 ms. This difference in the onset of acceleration can be attributed to the simple one-step chemistry model used in the work of Gamezo et al. [1]. Because as also commented by Liberman et al. [12] the chemical induction times estimated by the one-step model typically are a few times smaller than the reality. Another source of difference between the current work and that of Gamezo et al. [1] is the different laminar burning velocity calculated. This important parameter (especially in the initial time of flame propagation when the flame is laminar) depends on the models used for calculation of thermo-physical properties, thermo-chemical properties and chemical kinetics. Hence, it is expected that the laminar burning velocity predicted in the present work is different from that of Gamezo et al. [1].

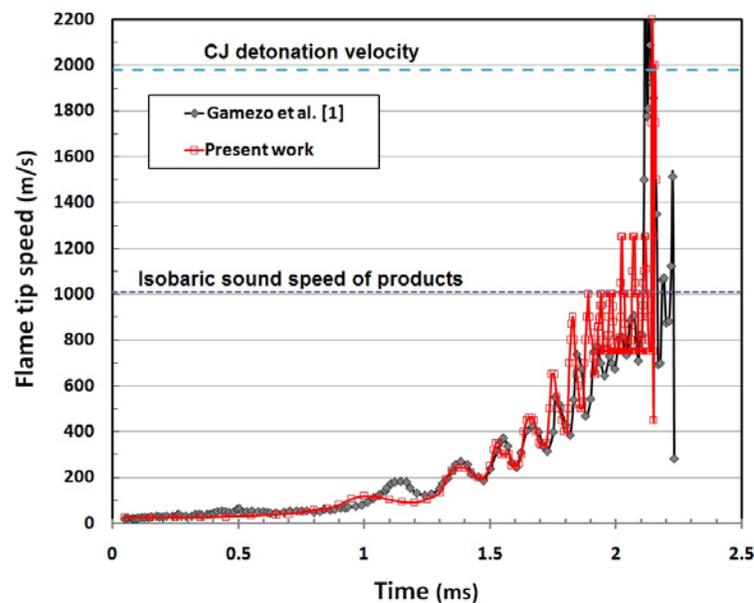


Figure 2. Comparison of the flame tip speed predicted in the present numerical work against the numerical prediction by Gamezo et al. [1].

## 4 Flame Acceleration and Fast Deflagration

Flame propagation speed is plotted versus the distance from ignition point in Fig. 3 (left). The flame acceleration continues until the speed of the flame reaches approximately the isobaric sound speed of the products (i.e., the choked regime). Then, transition from the choked regime to detonation occurs. When the flame passes the obstacle No. 6 the flame speed and the velocity of flow at a position ahead of the flame (typically in jet-like flow passing through the obstacles) increases up to a local sound speed of the compressed unburned gas. Consequently, a shock wave is formed in the domain. At this moment, a rapid decline in the flame surface area is observed (Fig. 3 (Right)). In the slow flame regime (before the obstacle No. 6) both the flame surface area and the flame speed increase. In this regime, the interaction of the vortex street ahead of the obstacles with the flame front leads to a considerable flame wrinkling. Hence, the flame acceleration is mainly due to the flame wrinkling [1, 2]. Although, after the obstacle No. 6 (where the flame relies in the fast flame regime) the behavior of the flame speed and flame surface area are in opposite. It means that the mechanism behind the fast flames propagation defer from the slow flames. When the flame speed reaches the sound speed of the compressed unburned mixture, the flow downstream of the further obstacles is not enhanced and gradually damped. Thus, the strong vortex fields are not formed ahead of the obstacles and as a result the extreme wrinkling that was observed in the slow flame propagation regime is not observed at these instants. To describe this discrepancy, the mean rate of energy release, averaged over the flame front is plotted versus the flame location in Fig. 4. In this figure, it is seen that the energy-release rate progressively increases as the flame passes obstacle No. 6. This leads to an increase in the rate of thermal expansion, which causes the flame acceleration.

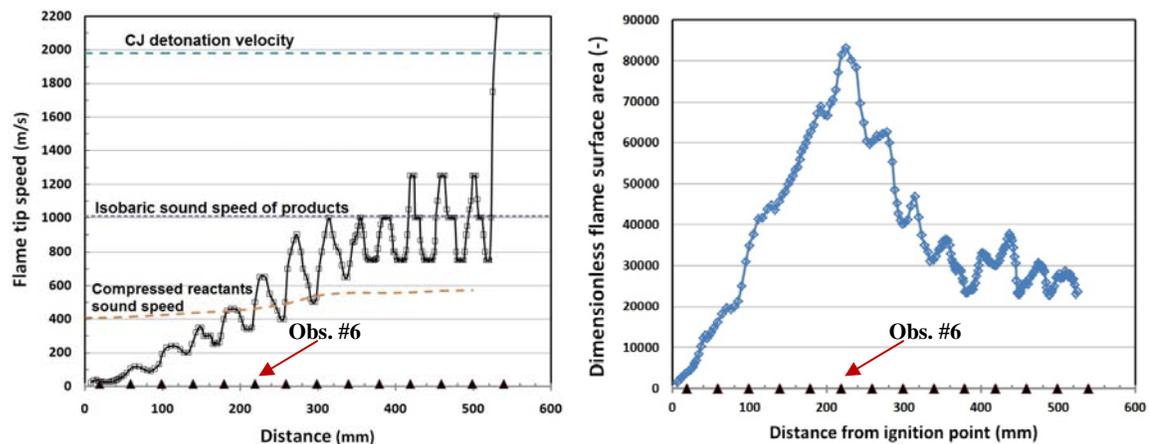


Figure 3. Left: flame tip speed against flame location from the ignition point. Right: dimensionless flame surface area as function of flame tip location. Obstacle locations are signed using triangular symbols.

In Fig. 5, shadowgraph picture and contours of the heat release rate, vorticity magnitude and turbulent velocity fluctuation are plotted on the flame front. In these snapshots it is clearly seen that in the fast flame regime, the interactions between the flame and reflected shocks from the channel walls and obstacles, enhances the heat release rate [3]. This phenomenon is clearly seen in Fig. 5. In this figure when the flame approaches obstacle No. 11 the interaction of leading edge of the flame with the reflected shocks from the obstacles results in an extreme

increase in the heat release rate. This is caused by a local increase of temperature and increase of the mixing in the flame front by Richtmyer-Meshkov (RM) instability due to baroclinic vorticity generation mechanism. The present observations are in agreement with the viewpoints of Ciccarelli and colleagues [13] about fast flame propagation mechanism. The present results indicate that in the fast flame regime, the main mechanism responsible for a high level enhancement of flame speed and maintaining the high heat release rate during the flame propagation is shock-flame interactions and the subsequent the RM instability.

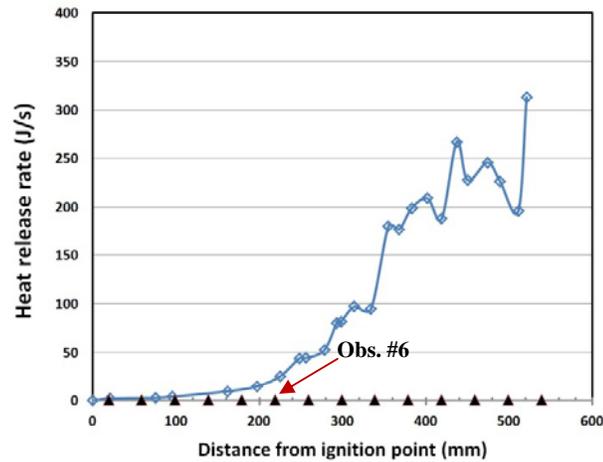


Figure 4. Averaged heat release rate (J/s) over the flame front as function of flame tip location.

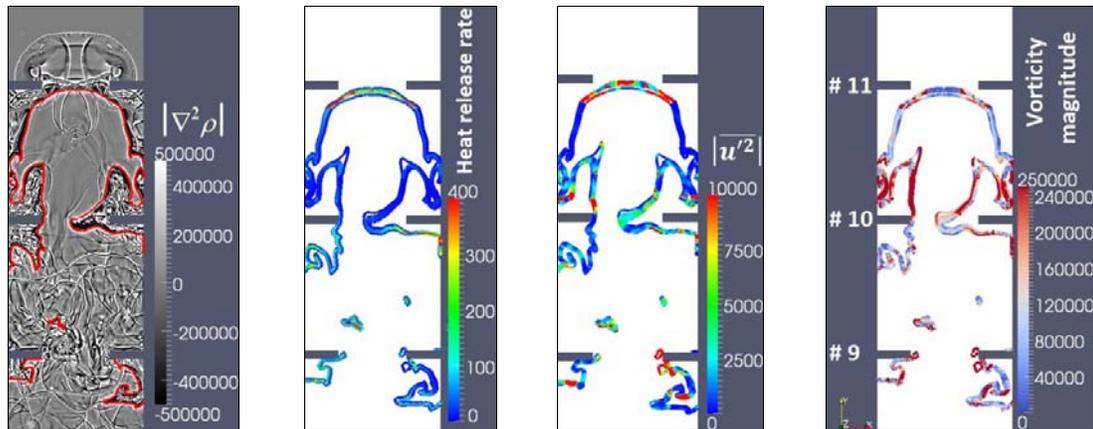


Figure 5. Time sequence of  $|\nabla^2\rho|$ , heat release rate (J/s), turbulent velocity fluctuations ( $|u'^2|$ ) and vorticity magnitude (1/s) fields respectively from left to right. These parameters have been mapped on the flame front. These images are corresponded to flame passes over the obstacle No. 11.

## 5 Conclusions

Using a detailed chemical kinetics, large eddy simulation was performed to examine the flame acceleration and propagation mechanism of fast deflagration in an obstructed channel filled

with premixed H<sub>2</sub>-Air mixture. The turbulence-chemistry interaction in SGS scales was represented using artificially thickened flame approach. To reduce the computational cost induced by the chemical kinetic, the ISAT method was exploited. The results showed that the LES/ATF/ISAT approach qualitatively well reproduces the behavior of a propagating flame during the subsonic and supersonic regimes. It is shown that in the fast flame regime, the flame surface area decreases rapidly, while the flame speed increases toward the choked regime. It is observed that the interactions between the flame and reflected shocks from the channel walls and obstacles, enhances the heat release rate and vorticity generation due to RM instability in the flame front (i.e., the baroclinic mechanism).

## References

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