1. INTRODUCTION

Until today, people have made efforts to enhance convective heat transfer by means of surface enlargement using obstacles such as ribs and fins and the increase in flow turbulence due to the interaction between the flow and the obstacles. However, additional pressure losses increase with introduction of obstacles and turbulence. The low thermal conductivity of conventional fluids such as water, oil, and of an ethylene glycol mixture is a serious limitation on improving the performance and compactness of this engineering equipment. To overcome the above-mentioned disadvantages, there is a strong motivation to develop advanced heat transfer fluids with substantially higher conductivity. An innovative way of improving the thermal conductivities of fluids is to suspend small solid particles in a fluid. Nanofluids are new heat transfer fluids containing a small quantity of nano-sized particles that are uniformly and stably suspended in a liquid. The dispersion of a small amount of solid nanoparticles in conventional fluids remarkably changes their thermal conductivity. Compared to the existing techniques for enhancing heat transfer, the nanofluids show a superior potential for increasing heat transfer rates in a variety of cases. In addition, flow in a lid-driven cavity or in a two-sided...
liddriven enclosure can be used in certain engineering applications such as electronic devices cooling, lubrication technologies, furnaces, chemical processing equipment, drying technologies, etc. Heat transfer and fluid flow properties have been studied previously in some of the works for rectangular or square cavities driven by buoyancy and shear forces. Oztop and Dagtekin (2004) investigated a mixed convection problem in a vertical two-sided liddriven differentially heated square cavity by a numerical method. The left and right moving walls were maintained at different constant temperatures, and the top and bottom walls were thermally insulated. The results have showed that both the Richardson number and the direction of the moving walls affect the fluid flow and heat transfer in the cavity. Luo and Yang (2007) have presented an extension of the method of calculating flow bifurcation with/without heat transfer in a cavity with opposite movement of top and bottom walls. Ouertatani et al. (2009) studied three-dimensional flow structures and heat transfer
rates in air within double lid-driven cubic cavity heated from the top and cooled from below numerically. The other walls were maintained adiabatic. They obtained that a remarkable heat transfer improvement of up to 76% can be reached for the case of Re = 400 and Ri = 1. Wahba (2009) simulated incompressible flow in two-sided and four-sided lid-driven cavities by a numerical method. For the two-sided lid-driven cavity, the upper wall moved to the right while the left wall moved downward with the speeds equal to that of the upper wall. At low Reynolds numbers, the flow field was symmetric with respect to one of the cavity diagonals for the two-sided lid-driven cavity, while for the four-sided lid-driven cavity, it proved to be symmetric with respect to both cavity diagonals. Many engineering electronic devices and mechanical instruments were limited by enhancing the performance and heat transfer rate in conventional fluids such as water, oil, and ethylene glycol mixtures. Primarily, of the reason is the low thermal conductivity of the active fluid. There are several procedures to develop heat transfer of fluids. An innovative way is improving the thermal conductivities of the active fluid by adding metallic nanoparticles to it, namely, the nanofluid, and consequently enhancing the heat transfer characteristics. In order to calculate the nanofluid properties, many models have been developed for estimating the thermal conductivity of nanofluids based on several parameters such as the geometry of nanoparticles, Brownian effects, temperature and interaction between nanoparticles and the base fluid (Karimipour, 2015; Zarringhalam et al., 2016; Esfe et al., 2015a; Akbari et al., 2016).

Maxwell (1904) proposed the first model for low-density mixtures with spherical particles. Based on the Maxwell model, the thermal conductivity of a nanofluid increases with increase in the volume fraction of solid nanoparticles. Many researchers investigated heat transfer and flow characteristics of a nanofluid in lid-driven enclosures (Karimipour et al., 2014; Eshgarf and Afrand, 2016; Esfe et al., 2014). Tiwari and Das (2007) numerically investigated the behavior of a copper–water nanofluid within a two-sided lid-driven differentially heated square cavity. The upper and bottom walls were insulated and the left and the right moving walls were maintained at constant temperatures. Three cases were studied based on the direction of movement of the walls. They found that the Richardson number, depicting the direction of the moving walls, affects the heat transfer and fluid flow in the cavity. Noor et al. (2009) investigated flow and heat transfer inside a square cavity with oscillating double side by a numerical procedure. Sivasankaran et al. (2010) performed a numerical study of mixed convection in a lid-driven cavity at different Prandtl numbers. The vertical sidewalls of the cavity were maintained with sinusoidal temperature distribution. The results showed that the heat transfer rate increased with the increasing amplitude ratio. It was observed that average Nusselt numbers were increased first, and then decreased when the phase deviation increased from 0 to π. The mixed convection heat transfer process, observed in double lid-driven cavities, is important in industrial applications and engineering designs. In many applications, the angle of cavity changes intentionally or involuntarily. Based upon the angle of the cavity, the lid-driven shear force may assist or oppose the buoyancy force and change the heat transfer rates. In addition, in order to enhance the heat transfer rate, an innovative technique replaces an active fluid by a nanofluid. Thus, in this paper, numerical study was performed in a SiO$_2$–water nanofluid within a square double lid-driven cavity with stationary cooled right wall and heated sinusoidal left wall. The diameter of the nanoparticles is assumed to be 100 nm. Since the nanofluid consists of very small-sized solid particles, at low solid concentration, it is reasonable to consider the nanofluid as a single-phase flow (Xuan and Li, 2000). The results were presented in the form of the stream contours, isotherm lines, and average Nusselt number. The purpose of this note is to enhance the discussion on the use of nanofluids with the sole aim of increasing the heat transfer coefficient in mixed convection flows in a square double lid-driven cavity with various inclination angles. The obtained results may have direct applications in industrial processes and technologies such as furnaces, lubrication technologies, drying technologies, chemical processing.
equipment, and others. More recent works can be referred to those involving nanofluid flow and heat transfer as like (Karimipour et al., 2011, 2015; Esfe et al., 2015b,c; Nikkhah et al., 2015; Akbari et al., 2015).

2. PROBLEM STATEMENT

Figure 1 shows a two-dimensional square double lid-driven cavity filled with a SiO$_2$–water nanofluid. The cavity is heated sinusoidally from the left wall and cooled from the right wall. Both top and bottom moving walls were thermally insulated. The cavity is subjected to top and bottom driven lids, and filled with a suspension of SiO$_2$ nanoparticles in water, with the diameters of nanoparticles equal to 100 nm. Since the nanofluid consists of very small solid particles, in low solid concentration, it is reasonable to consider the nanofluid as a single-phase flow.

Table 1 presents the thermophysical properties of water and SiO$_2$ at the reference temperature. It is assumed that the base fluid and the nanoparticles are in thermal equilibrium, and that there is no slip between

![FIG. 1: Schematic diagram of the physical system](image)

<table>
<thead>
<tr>
<th>TABLE 1: Thermophysical properties of different phases</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Physical Properties</strong></td>
</tr>
<tr>
<td>$c_p$, J/kg·K</td>
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<tr>
<td>$\rho$, kg/m$^3$</td>
</tr>
<tr>
<td>$k$, W·m$^{-1}$·K$^{-1}$</td>
</tr>
<tr>
<td>$\alpha \times 10^5$, 1/K</td>
</tr>
<tr>
<td>$\beta \times 10^3$, 1/K</td>
</tr>
<tr>
<td>$\mu \times 10^4$, kg/m·s</td>
</tr>
</tbody>
</table>
them, and the shape and size of solid particles are uniform. Except for the density, the properties of the nanoparticles and fluid are taken to be constant. In addition, we neglect the viscous dissipation in the governing equations.

3. GOVERNING EQUATIONS

The governing equations for the steady, 2D laminar and incompressible mixed convection flow are expressed as follows:

\[ \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0, \quad (1) \]

\[ u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = -\frac{1}{\rho_{nf}} \frac{\partial p}{\partial x} + \nu_{nf} \nabla^2 u + \frac{(p\beta)_{nf}}{\rho_{nf}} g \sin (\gamma)(T - T_c), \quad (2) \]

\[ u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} = -\frac{1}{\rho_{nf}} \frac{\partial p}{\partial y} + \nu_{nf} \nabla^2 v + \frac{(p\beta)_{nf}}{\rho_{nf}} g \cos (\gamma)(T - T_c), \quad (3) \]

\[ u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} = \alpha_{nf} \nabla^2 T. \quad (4) \]

The following dimensionless parameters are used to obtain the dimensionless form of the governing equations:

\[ X = \frac{x}{L}, \quad Y = \frac{y}{L}, \quad V = \frac{v}{u_0}, \quad U = \frac{u}{u_0}, \quad \Delta T = T_h - T_c, \quad \theta = \frac{T - T_c}{\Delta T}, \quad P = \frac{p}{\rho_{nf}u_0^2}, \quad (5) \]

where \( T_h \) is the maximum temperature of the left wall surface calculated from the definition of the Ra number. Reynolds number and other parameters are defined as follows:

\[ \text{Re} = \rho_f u_0 L \frac{u_0}{\mu_f}, \quad \text{Pr} = \frac{\nu_f}{\alpha_f}, \quad \text{Ra} = \frac{g B_f \Delta T L^3}{\nu_f \alpha_f}, \quad \text{Gr} = \frac{Ra}{Pr}, \quad \text{Ri} = \frac{Gr}{Re^2}. \quad (6) \]

The thermal diffusivity and effective density of the nanofluid are given by

\[ \alpha_{nf} = \frac{k_{nf}}{(p c_p)_{nf}}, \quad (7) \]

\[ \rho_{nf} = \varphi \rho_p + (1 - \varphi) \rho_f. \quad (8) \]

The heat capacitance and the thermal expansion coefficient of the nanofluid are defined as

\[ (p c_p)_{nf} = \varphi (p c_p)_p + (1 - \varphi) (p c_p)_f, \quad (9) \]

\[ (p\beta)_{nf} = \varphi (p\beta)_p + (1 - \varphi) (p\beta)_f. \quad (10) \]
The viscosity of the nanofluid is estimated by using the Brinkman model given by

$$\mu_{nf} = \frac{\mu_f}{(1 - \varphi)^{2.5}}. \quad (11)$$

Several relations can be used for the expression of the effective thermal conductivity of the nanofluid. In this study, the model of Patel et al. (2005) is used to determine the thermal conductivity of the nanofluid:

$$\frac{k_{nf}}{k_f} = 1 + \frac{k_p A_p}{k_f A_f} + ck_p Pe \frac{A_p}{k_f A_f}. \quad (12)$$

The parameter $c$ is equal to 25,000. Other parameters used are defined here as

$$\frac{A_p}{A_f} = \frac{d_f d_p}{1 - \varphi}, \quad Pe = \frac{u_p d_p}{\alpha_f}, \quad u_p = \frac{2k_b T}{\pi \mu_f d_p^2}, \quad d_p = 100 \text{ nm}, \quad d_f = 2 \text{ Å}. \quad (13)$$

In order to investigate the effects of different parameters on heat transfer, the local Nusselt number is defined as follows:

$$Nu = \frac{hL}{k_f}, \quad (14)$$

where the heat transfer coefficient is

$$h = \frac{q^*}{T_h - T_c}. \quad (15)$$

The value of the heat flux over the cold wall is expressed as

$$q^* = -k_{nf} \frac{\partial T}{\partial x}. \quad (16)$$

By substituting Eqs. (15) and (16) into Eq. (14), the local Nusselt number can be written as

$$Nu = -\frac{k_{nf}}{k_f} \frac{\partial \theta}{\partial X}. \quad (17)$$

The average Nusselt number over the cold surface is expressed as follows:

$$Nu_m = \frac{1}{L} \int_0^L Nudx'. \quad (18)$$

The boundary conditions are as follows:

left wall:

$$\begin{cases}
U = V = 0 \\
T(y') = T_c + (T_h - T_c) \sin \left( \frac{\pi y'}{L} \right) \rightarrow \theta = \sin(\pi Y);
\end{cases} \quad (19)$$

right wall:

$$\begin{cases}
U = V = 0 \\
\theta = 0;
\end{cases} \quad (20)$$
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4. NUMERICAL METHOD

The continuity, momentum, and energy balance equations have been solved using the control-volume numerical code and the SIMPLER algorithm (Brinkman, 1958) used for the pressure–velocity coupling. In order to assess the accuracy of the results, a complete study has been carried out with the use of Basak et al.’s (2009) model. Figure 2 shows some results in the form of temperature contours for the uniform bottom heating case with $\text{Re} = 100$, $\text{Gr} = 10^4$, $\text{Pr} = 0.7$ (left figure) and $\text{Pr} = 10$ (right figure). The diagrams are in accordance.

To study the effect of the grid size on the results, two cases were investigated by changing the number of grid points in uniform mesh. The results of this study are presented in Table 2 for various cases. Grid independence was achieved within the grid size of $121 \times 121$.

5. RESULTS AND DISCUSSION

For extreme combinations of high $\text{Ri}$ and low $\text{Re}$ numbers, heat transfer is substantially dominated by conduction. For extreme combinations of small $\text{Ri}$ and high $\text{Re}$ numbers, the dominant heat transfer becomes convective. In this paper, natural and forced convection were investigated. The top and bottom walls were adiabatic moving to right and left, respectively. The left wall had a sinusoidal temperature and the right wall had a low temperature $T_c$. The stream function, isotherm lines, and the average Nusselt number were presented for the SiO$_2$–water nanofluid for $0.1 < \text{Ri} < 10$, $1 < \text{Re} < 100$, $0.0 < \phi < 0.06$, and $0^\circ < \gamma < 150^\circ$.

FIG. 2: Temperature contours for uniform bottom heating case with $\text{Re} = 100$, $\text{Gr} = 10^4$, $\text{Pr} = 0.7$ (left figure) and $\text{Pr} = 10$ (right figure) for current study (…) and Basak et al. (2009) (—)
Figure 3 presents streamlines and temperature field for $Ri = 2$ for both the base fluid ($\phi = 0$) and nanofluid ($\phi = 0.06$). It is observed that a single recirculation eddy dominates the cavity. The intensity of streamlines near the moving walls is high, and a vertical circulation is created in the center of the enclosure. By increasing the Reynolds number from 1 to 100, the nanofluid moves faster in the horizontal direction, the width of the vertical circulation increases, and the streamlines accede to the hot and cold surfaces and thus, heat transfer increases because of the enhancement in the rate of flow passing near hot and cold surfaces. For all angles other than $150^\circ$ and $Re = 100$, a single recirculation eddy is observed in the cavity. At $\gamma = 150^\circ$ and $Re = 100$ a circulation in the cavity and a small vortex are created at the bottom of the hot wall. Because at $\gamma = 120^\circ$ and $150^\circ$ the heated nanofluid moves upward, while the driven lids cause the movement of the nanofluid in the opposite direction from the buoyancy force, towards the bottom. When the cavity inclination angle changes from zero to $150^\circ$, the circulation flow in the cavity becomes weaker. Increment in solid volume fraction does not cause noticeable changes in the streamline contours, but streamlines in some cases at $Re = 100$ approach the left and right walls. At $Re = 100$ and $\gamma = 150^\circ$, by increasing the solid volume fraction, the size of the small vortex decreases and streamlines approach the wall surfaces.

The form of the isotherm lines near the hot wall is due to the sinusoidal distribution of temperature on a heat source. The isotherm line has such a form because the temperature in the center of the hot wall is at its highest value and has the lowest value near the top and bottom wall. The nanofluid beside the hot wall expands and moves towards the upper wall due to the buoyancy force. As mentioned before, the upper part of the hot wall has a lower temperature than the middle of the wall. So, the finally heated nanofluid faces the part of the wall with a lower temperature, and this leads to the transfer of the amount of heat from the hot nanofluid to the wall. Therefore, the amount of net heat transfer of the left wall is reduced. By increasing the Re number at a particular inclination angle and the Richardson number, the temperature gradient near the surface increases. Therefore, the local heat transfer from the middle and top of the hot wall increases and a transaction is created between local heat transfers. For $Re = 1$, the isotherm lines are almost parallel in the right part of the cavity. In this part of the cavity, there is conductive heat transfer between the vertical layers of the nanofluid, which changes to conductive heat transfer between the horizontal layers near the top and bottom walls by changing the Re number from 1 to 100. By increasing the inclination angle at a lower Reynolds number, small changes in the isotherm lines are observed. Both natural and forced heat transfer are important at $Ri = 2$. Because of the low Re numbers, the conductive heat transfer dominates. Therefore, the change in the inclination angle does not affect much the temperature lines. At $\gamma = 0^\circ$, the forces caused by the moving lids and the buoyancy act in the same direction in which the temperature of the heated fluid de-

<table>
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<tr>
<th>$\phi = 0.06$, $Re = 100$, $Ri = 10$, $\gamma = 150^\circ$</th>
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<td>6.225</td>
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</tr>
<tr>
<td>6.232</td>
<td>0.717</td>
<td>141 × 141</td>
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</tbody>
</table>
FIG. 3: Flow pattern and thermal fields for $Ri = 2$, base fluid (−), and nanofluid with $\phi = 0.06$ (−−−)
creases due to its contact with the colder part of the left wall. The buoyancy force always acts in the vertical direction, and the forced convection acts tangentially to the wall surfaces. By increasing $\gamma$, the heated nanofluid gets away from the hot wall, which has a lower temperature in comparison with the nanofluid at the upper portion. Therefore, the value of the isotherm lines at a distance from the hot wall increases at a higher inclination angle. This behavior is more obvious at $\gamma = 150^\circ$. When $\phi$ increases from 0 to 0.06, the isotherm lines get closer to the hot heat source surface near the hot or cold walls. Figure 4 shows the streamlines for various Ri and Re numbers for $\gamma = 30^\circ$. By increasing the Re number from 1 to 100, a stronger flow field is produced in the cavity. When the Ri number is altered from 0.1 to 10, the conduction and natural convection increase. Because the buoyancy and shear forces are aiding each other for $\gamma = 30^\circ$, the intensity of streamlines increases near the walls and the circulation in the cavity becomes stronger. Increment in $\phi$ generally causes stronger circulation.

Isotherm lines are presented in Fig. 5 for $\gamma = 30^\circ$. With increase in the Re or Ri number, the isotherm lines get closer to the hot and cold walls. Therefore, the temperature gradient increases especially near the cold wall as the heat transfer does. Increment in nanoparticle causes two different behaviors in the isotherm lines. It is observed that some pieces of lines approach the walls but other pieces get away because of the sinusoidal distribution of temperature in the hot wall surface.

Figure 6 presents average Nusselt numbers for all the cases studied. An average Nusselt number has very small variation at very low Re and Ri. At Re = 1, by increasing the Ri number from 0.1 to 10, the values of $\text{Nu}_m$ decrease a little for $\gamma = 120^\circ$ and $150^\circ$, and increase for $\gamma = 0^\circ$, $30^\circ$, and $60^\circ$. At $\gamma = 90^\circ$, the values of $\text{Nu}_m$ remain constant. At Re = 10, natural convection increases with increasing Ri, and buoyancy force moves the nanofluid upward while forced convection moves the nanofluid near the walls. Thus, the average Nusselt number decreases by increasing the inclination. At Re = 10, $\text{Nu}_m$ increases while Ri changes from 0.1 to 10 for $0^\circ \leq \gamma \leq 120^\circ$, and decreases at $\gamma = 150^\circ$. Generally, an enhancement in $\text{Nu}_m$ is observed by changing the Ri number from 0.1 to 10 for all $\gamma$ values at Re = 100. Only a decrease in $\text{Nu}_m$ occurs for $\gamma = 150^\circ$ and $120^\circ$ by increasing Ri from 0.1 to 2.

At Re = 1, the values of $\text{Nu}_m$ decrease by increasing the inclination angle for all Ri numbers. The highest variation of $\text{Nu}_m$ with Ri is observed at $\gamma = 0^\circ$. Slope of $\text{Nu}_m$–Ri decreases by enhancing $\gamma$ until a low slope at $\gamma = 120^\circ$ and then negative slope (decreases in $\text{Nu}_m$) at $\gamma = 150^\circ$ is observed. The average Nusselt number increases by changing $\gamma$ from 0 to $30^\circ$ and decreases by more increase in $\gamma$ for all Ri numbers and Re = 10. $\text{Nu}_m$ increases at Re = 100 by increasing $\gamma$ from $0^\circ$ to $30^\circ$ for all Ri numbers and decreases by changing $\gamma$ from $30^\circ$ to $150^\circ$ for Ri = 0.1 and 2, and $\gamma = 30^\circ$ to $90^\circ$ for Ri = 7 and 10. By changing the $\gamma$ value from $90^\circ$ to $120^\circ$, it is observed that $\text{Nu}_m$ increases extremely and then decreases a little for $\gamma = 150^\circ$ relative to $120^\circ$. Figure 7 shows streamlines and isotherms for $\gamma = 150^\circ$, Re = 100, $\gamma = 0.06$, and Ri = 2, Ri = 7, and Ri = 10. According to Fig. 7, three circulations are created in the cavity for Ri = 7 and 10, while at Ri = 2, only one main circulation exists, because at Ri = 2, the buoyancy force is weaker than at Ri = 7 and Ri = 10. Thus, by augmenting the Ri number from 2 to 7 and 10, the buoyancy force causes the fluid to move upward (perpendicular to the surface), while the driven lids cause the fluid to move near the surfaces. Because of the two strong forces, three circulations are created in the cavity, while at Ri = 2, as mentioned, the buoyancy force is weaker than at Ri = 7 as shear forces are created by the driven lids at Ri = 2. Thus, shear forces conquest the buoyancy force and a main circulation in the cavity and a small circulation near the hot surface — in the middle of the wall because of sinusoidal distribution — are created. It is observed from Fig. 7 that by increasing the Ri number, the intensity of temperature lines near the cold wall increases, and the heated fluid rises from the hot surface. Hence, the average Nusselt numbers increase by increasing the nanoparticle volume fraction for all the cases studied.
FIG. 4: Flow pattern at $\gamma = 30^\circ$, base fluid (—), and nanofluid with $\varphi = 0.06$ (- - -).


**FIG. 5**: Thermal fields at $\gamma = 30^\circ$, base fluid (—), and nanofluid with $\varphi = 0.06$ (-----)

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<table>
<thead>
<tr>
<th>$Re$</th>
<th>$Ex=1$</th>
<th>$Ex=10$</th>
<th>$Ex=100$</th>
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<tbody>
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<td><img src="image11.png" alt="Image" /></td>
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</table>
FIG. 6: Average Nusselt numbers at γ = 0° for all of the cases studied.
6. CONCLUSIONS

In this study, mixed convection flows through a nanofluid in a square double lid-driven cavity with various inclination angles was carried out. The cavity was nonuniformly heated from the left, $T_h$, and cooled from the opposite wall. The top and the bottom moving walls were insulated. The study was conducted for the Richardson number 0.1 to 10, Reynolds number 1 to 100, while solid volume fractions ($\phi$) of nanoparticles were altered from 0 to 0.06.

In view of the results obtained, the following findings may be summarized:

- By increasing the Reynolds number from 1 to 100, nanofluid moves faster in the horizontal direction and streamlines accede to the hot and cold surfaces and heat transfer increases because of the enhancement in the rate of flow passing near the hot and cold surfaces.
- By increasing the Re number from 1 to 100, a stronger flow field is produced in the cavity.
- When the Ri number is altered from 0.1 to 10, the conduction and natural convection increase.
- Because the buoyancy and shear forces are aiding each other for $\gamma = 30^\circ$, the intensity of streamlines increases near the walls, and the circulation in the cavity becomes stronger.
- Increment in $\phi$ generally causes a stronger circulation.
• With increase in the Re or Ri number, the isotherm lines get closer to the hot and cold walls.
• The temperature gradient increases especially near the cold wall as the heat transfer does.

Further studies aimed at elucidation of the precise nature of this flow regime would be of considerable interest. In addition, more investigations are called for in order to find out the reasons that lead to heat transfer deterioration in nano-fluids. The extension of this study on the basis of previous works (Noorian et al., 2014a,b; Rezaei et al., 2015a,b; Semiromi and Azimian, 2010a,b,c; Semiromi and Azimian, 2012; Toghraie et al., 2016a,b; Toghraie and Azimian, 2009) affords engineers an opportunity for conducting simulations and experimental investigations.

REFERENCES


